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Total No. of Pages : 02

Total No. of Questions : 08

**M.Tech. (ME) (Sem.-1)**  
**FINITE ELEMENT ANALYSIS**  
**Subject Code : MTME-102**  
**M.Code : 74716**  
**Date of Examination : 16-05-2023**

Time : 3 Hrs.

Max. Marks : 100

**INSTRUCTIONS TO CANDIDATES :**

1. Attempt any FIVE questions in all.
2. Each question carries TWENTY marks.

1. Analyse a simply supported beam subjected to a uniformly distributed load throughout using Rayleigh Ritz method. Adopt one-parameter trigonometric function. Evaluate the maximum deflection and bending moment and compare with the exact solution.
2. Write short note on the following :
  - a) Natural coordinates in FEA
  - b) Use of Numerical integration in FEA
  - c) Stream function-vorticity formulation
  - d) Viscous flow and incompressible flow.
3. For the plane strain elements shown in Fig. 1, the nodal displacements are given as  $u_1 = 0.005$  mm,  $v_1 = 0.002$  mm,  $u_2 = 0.0$  mm,  $v_2 = 0.0$  mm,  $u_3 = 0.005$  mm,  $v_3 = 0.30$  mm. Determine the element stresses and the principle angle. Take  $E = 70$  GPa and Poisson's ratio = 0.3 and use unit thickness for plane strain. All coordinates are in mm.

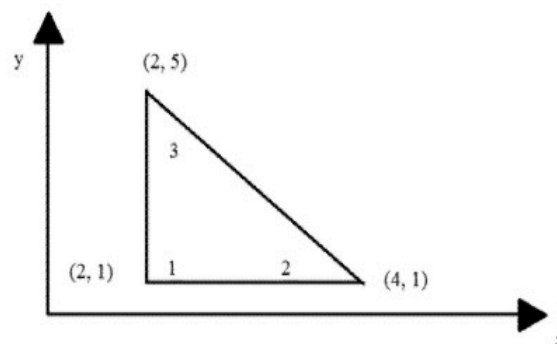


Fig. 1

4. A metallic fin 20 mm wide and 4 mm thick, is attached to a furnace whose wall temperature is  $180^{\circ}\text{C}$ . The length of the fin is 120 mm. If the thermal conductivity of the material of the fin is  $350 \text{ W/m}^{\circ}\text{C}$  and convection coefficient is  $9 \text{ W/m}^2\text{ }^{\circ}\text{C}$ , determine the temperature distribution assuming that the tip of the fin is open to the atmosphere and that the ambient temperature is  $25^{\circ}\text{C}$ .

5. Solve the ordinary differential equation  $(d^2y/dx^2) + 10x^2 = 0$  for  $0 \leq x \leq 1$

Subject to the boundary conditions  $y(0) = y(1) = 0$  using the Galerkin method with the trial functions  $N_0(x) = 0$  ;  $N_1(x) = x(1 - x^2)$ .

6. A concentrated load  $P = 50 \text{ kN}$  (Fig. 2) is applied at the centre of a fixed beam of length 3 m, depth 200 mm and width 120 mm. Calculate the deflection and slope at the midpoint. Assume  $E = 2 \times 10^5 \text{ N/mm}^2$ .

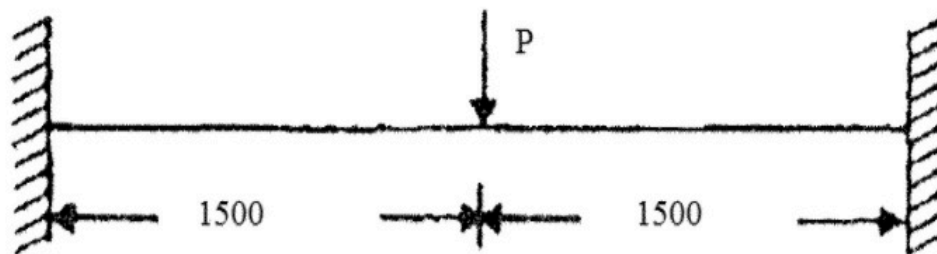


Fig. 2

7. Develop a one-dimensional finite element model of heat transfer including both conduction and convection for a solid cylindrical body surrounded by a fluid medium. Assume boundary conditions.
8. a) What are the non-zero strain and stress components of axis symmetric element? Explain.
- b) Derive the stiffness matrix of an axis symmetric element using potential approach.

**NOTE : Disclosure of Identity by writing Mobile No. or Making of passing request on any page of Answer Sheet will lead to UMC against the Student.**