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Total No. of Pages : 02

Total No. of Questions : 09

# M.Sc (Physics) (Sem.–2) MATHEMATICAL PHYSICS - II Subject Code : MSPH-421-21 M.Code : 91902 Date of Examination : 12-12-22

Time : 3 Hrs.

Max. Marks : 60

## **INSTRUCTIONS TO CANDIDATES :**

- 1. SECTION-A is COMPULSORY consisting of TEN questions carrying TWO marks each.
- 2. SECTION-B contains FIVE questions carrying FIVE marks each and students have to attempt any FOUR questions.
- 3. SECTION-C contains THREE questions carrying TEN marks each and students have to attempt any TWO questions.

## **SECTION-A**

- 1. Write briefly :
  - a) What is a cyclic group?
  - b) What do you understand by isomorphism in group theory?
  - c) 'A coset is not a group'. Discuss.
  - d) What are infinite Fourier sines and cosine transforms?
  - e) Write down Parseval's identity for Fourier series.
  - f) What are Neumann boundary conditions?
  - g) Define Quotient rule of tensors.
  - h) Write two properties of Laplace transform.
  - i) Define Gibbs phenomenon.
  - j) State Hilbert-Schmidt theory.

#### **SECTION-B**

- 2. Find the Fourier transform of a Gaussian distribution function  $f(x) = Ne^{-\alpha x^2}$  where N and  $\alpha$  are constants.
- 3. Find fourier series of the function  $e^x$  in the interval  $-\pi < x < \pi$ .
- 4. What are Topological groups and Lie groups? Give examples to explain.
- 5. State and prove four properties of inverse Laplace transforms.
- 6. Discuss the importance of Green's function in one dimension.

#### **SECTION-C**

- 7. Obtain Fourier series for the expansion  $f(x) = x \sin x$  in the interval  $-\pi < x < \pi$ . Hence prove that  $\frac{\pi}{4} = \frac{1}{2} + \frac{1}{1.3} \frac{1}{3.5} + \frac{1}{5.7} \dots$
- 8. a) Obtain expressions for  $a_0$ ,  $a_n \& b_n$  in Fourier series expansion of a function.
  - b) Prove that the Fourier transform of a Gaussian is another Gaussian.
- 9. a) Prove that symmetric transformation of square form a group.
  - b) What are conjugate classes? Discuss the multiplication of two classes.

NOTE : Disclosure of Identity by writing Mobile No. or Making of passing request on any page of Answer Sheet will lead to UMC against the Student.