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Total No. of Pages : 02

Total No. of Questions : 08

M.Sc. (Mathematics) (2018 Batch) (Sem.-1)

ALGEBRA-I

Subject Code : MSM-101-18

M.Code : 75129

Time : 2 Hrs.

Max. Marks : 35

INSTRUCTIONS TO CANDIDATES :

1. Attempt any FIVE question(s), each question carries 7 marks.
  - a) Let  $G$  be a Group such that  $(ab)^2 = a^2b^2$  for all  $a, b \in G$  show that  $G$  is abelian.
  - b) If  $a, b$  are any two elements in group  $G$ , Show that  $ab$  and  $ba$  have the same order.
2.
  - a) Define normal series of group  $G$ .
  - b) State all Sylow theorems.
3.
  - a) State and prove third isomorphism theorem.
  - b) Prove that set  $\text{Aut}(G)$  of all automorphisms of a Group  $G$  is a group under composition of mapping and  $\text{In}(G) \trianglelefteq \text{Aut}(G)$ .  
Prove that alternating group  $A_n$  is simple for  $n > 4$ .
4.
  - a) State and prove Jordan – holder’s theorem.
5.
  - b) Prove that every permutation can be expressed as a product of transpositions.
6.
  - a) In a non zero commutative ring with unity. Prove that ideal  $M$  is maximal if and only if  $R/M$  is a field.
  - b) If  $R$  is a Ring with unity. Show that each maximal ideal is prime. But the converse in general, is not true.
7. State and prove fundamental theorem of homomorphism.
8. State and prove fundamental theorem on finitely generated abelian groups.

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Student found sharing the question paper(s)/answer sheet on digital media or with

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