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Total No. of Pages : 03

Total No. of Questions : 07

B.Sc.(Computer Science) (Sem.–5)

NUMERICAL ANALYSIS

Subject Code : BCS-501

M.Code : 72574

Date of Examination : 12-12-22

Time : 3 Hrs.

Max. Marks : 60

INSTRUCTIONS TO CANDIDATES :

1. SECTION-A is COMPULSORY consisting of TEN questions carrying TWO marks each.
2. SECTION-B contains SIX questions carrying TEN marks each and students have to attempt ANY FOUR questions.

SECTION-A

1. Write briefly :

- a) If $u = \frac{5xy^2}{z^3}$ and errors in x , y and z be 0.001. Compute the relative maximum error in u when $x = y = z = 1$.
- b) If true value of a number is 36.25 and its absolute error is 0.002. Find the relative error and percentage error.
- c) In the method of false position, state the formula for the first approximation of the root of given equation, where symbol have their usual meaning.
- d) What is the difference between Gauss-Seidal and Jacobi's method?
- e) Find the root of the equation $x^3 - x - 1 = 0$ lying between 1 and 2 up to first iteration using Bisection method.
- f) Define Milne's predictor corrector method?
- g) Find the unique polynomial $P(x)$ of degree 2 or less such that
 $P(1) = 1$, $P(3) = 27$, $P(4) = 64$
using Newton divided difference formula.
- h) What is the formula for Simpson's rule?

- i) State normal equations for fitting a second degree polynomial $y = a + bx + cx^2$.
- j) Define Adams-Bashforth predictor corrector equations?

SECTION-B

2. Compare a real root of the equation:

$$f(x) = 3x + \sin(x) - e^x = 0, x_0 = 0, x_1 = 1$$

using Regula-Falsi Method.

3. Find the inverse of coefficient matrix of the given set of equations by Gauss-Jordan method with partial pivoting and hence solve the system.

$$x_1 + x_2 + x_3 = 1$$

$$4x_1 + 3x_2 - x_3 = 6$$

$$3x_1 + 5x_2 + 3x_3 = 4$$

4. Apply Gauss's forward formula to obtain $f(32)$ given that $f(25) = 0.2707, f(30) = 0.3027, f(35) = 0.3386, f(40) = 0.3794$.
5. Find the solution at $x = 12.2$ using Stirling's formula.

| x | 10 | 11 | 12 | 13 | 14 |
|------|---------|--------|---------|---------|---------|
| f(x) | 0.23967 | 0.2806 | 0.31788 | 0.35209 | 0.38368 |

6. Using the Adams-Bashforth predictor-corrector equations, evaluate $y(1.4)$, if y satisfies the following equation:

$$\frac{dy}{dx} + \frac{y}{x} = \frac{1}{x^2}$$

and $y(1) = 1, y(1.1) = 0.996, y(1.2) = 0.986, y(1.3) = 0.972$.

7. Given $y' = x^3 + y, y(0) = 2$, compute $y(0.2), y(0.4)$ and $y(0.6)$ using the Runge-Kutta Method of fourth order.

NOTE : Disclosure of Identity by writing Mobile No. or Making of passing request on any page of Answer Sheet will lead to UMC against the Student.